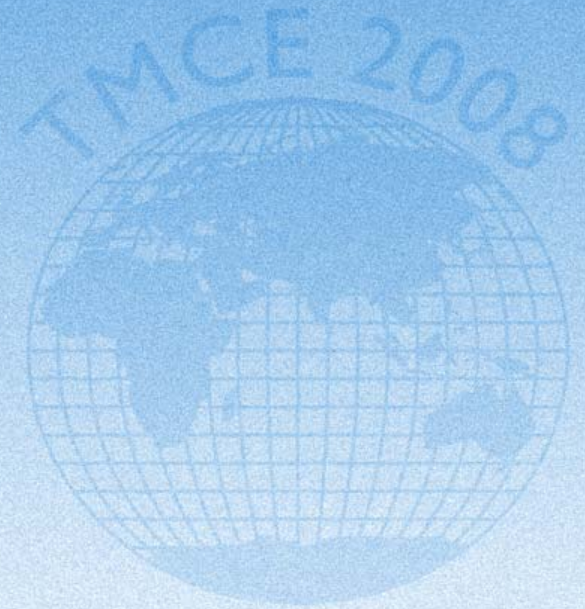


# CUTTING PROCESS OPTIMIZATION ON THE BASE OF CNC ADAPTIVE PROGRAMMING

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[www.cadcam.ge](http://www.cadcam.ge)



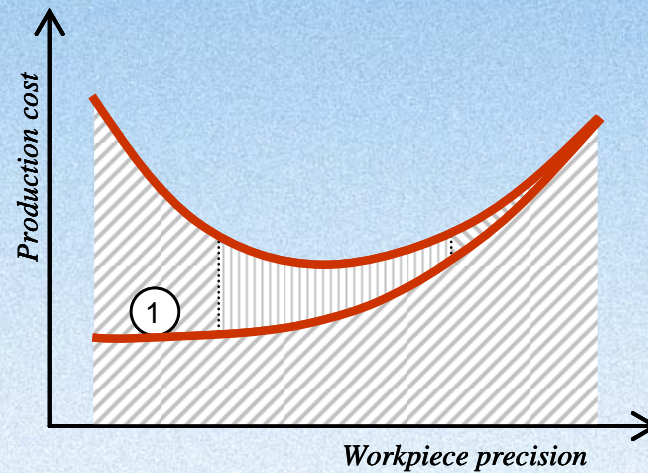
**TMCE 2008** April 21 – 25 Izmir, Turkey

# Total production cost

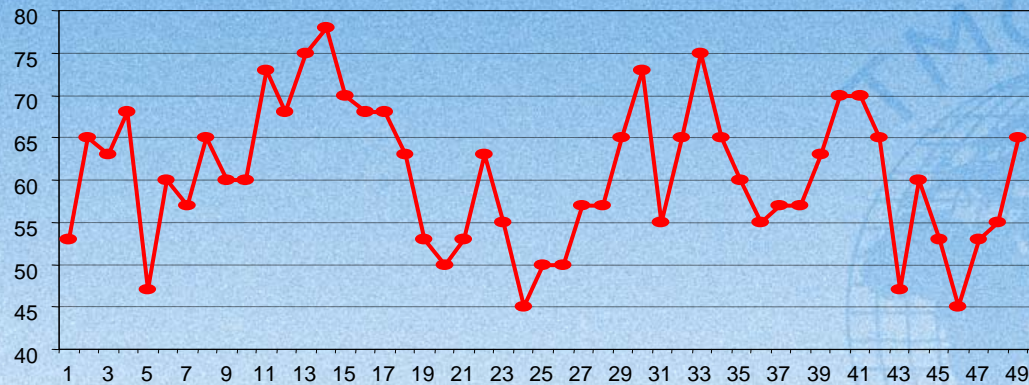
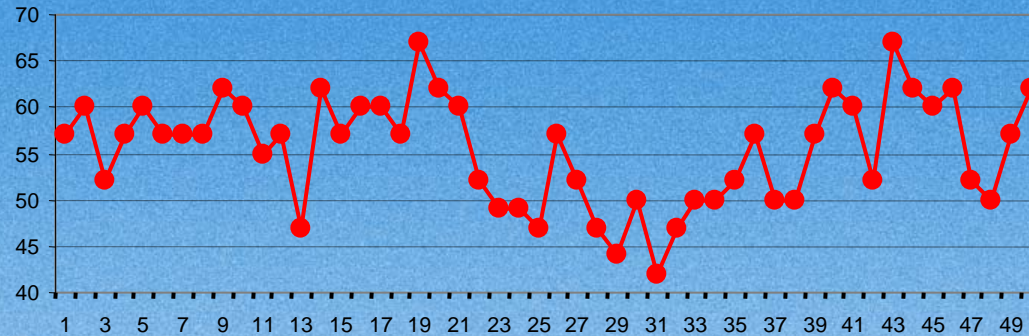
$$Q_{\Sigma} = Q_W + Q_M$$

$Q_W$  - cost of workpiece

$Q_M$  - cost of machining



# Dispersion of Workpiece Hardness:



Deviation from average is for:

- ▶ Iron alloys – 46%
- ▶ Aluminum alloys – 48%

# Dispersion of Workpiece Dimensions:

## Engineering hand books

Types	$(R_z)_1$ (mm)	$h_1$ (mm)	$(\Delta\Sigma)_1$ (mm)		$(Td)_1$ (mm)	$\varepsilon_1$ (mm)	
CASTING	0.2	0.1	0.28		4	2.6	
PUNCHING	0.2	0.25	$\frac{\Delta_k}{0.084}$	$\frac{\Delta_0}{1}$	1.1	5	4
ROLLING	0.32	0.4	2.1		3	4.32	
WELDING	1.5	-	$\frac{\Delta_k}{0.06}$	$\frac{\Delta_0}{1}$	1.06	5.5	5.3

## Manufacturing experience

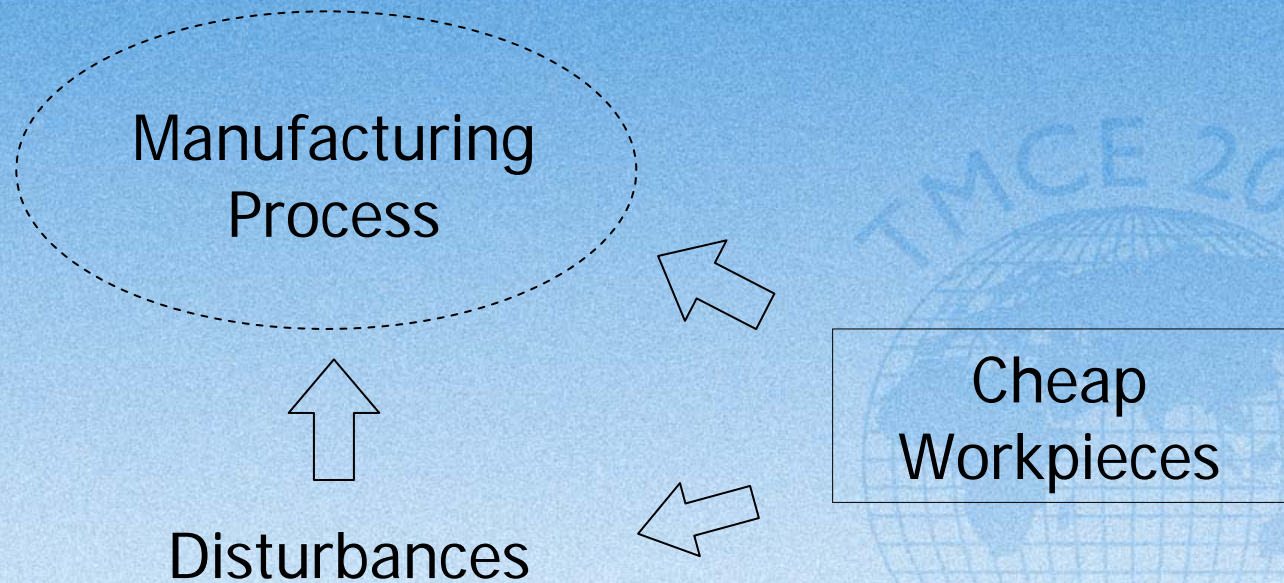
Types	$(R_z)_1$ (mm)	$h_1$ (mm)	$(\Delta\Sigma)_1$ (mm)	$(Td)_1$ (mm)	$\varepsilon_1$ (mm)
CASTING	$(R_z)_1$	$h_1$	$(\Delta\Sigma)_1$	4	2.6
PUNCHING	$(R_z)_1$	$h_1$	$(\Delta\Sigma)_1$	4.2	3.7
ROLLING	-	-	-	-	-
WELDING	$(R_z)_1$	$h_1$	$(\Delta\Sigma)_1$	11	8.1

## Literature sources

Types	$(R_z)_1$ (mm)	$h_1$ (mm)	$(\Delta\Sigma)_1$ (mm)	$(Td)_1$ (mm)	$\varepsilon_1$ (mm)
CASTING	$(R_z)_1$	$h_1$	0.21	2.6	1.8
PUNCHING	0.2	1	$(\Delta\Sigma)_1$	2.4	3.5
ROLLING	$(R_z)_1$	0.75	$(\Delta\Sigma)_1$	$(Td)_1$	4.7
WELDING	-	3.5	5.6	15.3	16.8

	Hand-Books $\varepsilon_1$ (mm)	Experience $\varepsilon_2$ (mm)	Sources $\varepsilon_3$ (mm)
CASTING	2.6	2.6	1.8
PUNCHING	4	3.7	3.5
ROLLING	4.32	-	4.7
WELDING	5.3	8.1	16.8

Disturbance is the difference between the designed and existing values of workpiece parameters



# Methods of Parametrical Optimization

*Without* considering  
of expences of tools

*With* considering of  
wear of tools

$$T = \frac{C_T}{V^\mu \cdot S^\nu \cdot t^\rho}$$

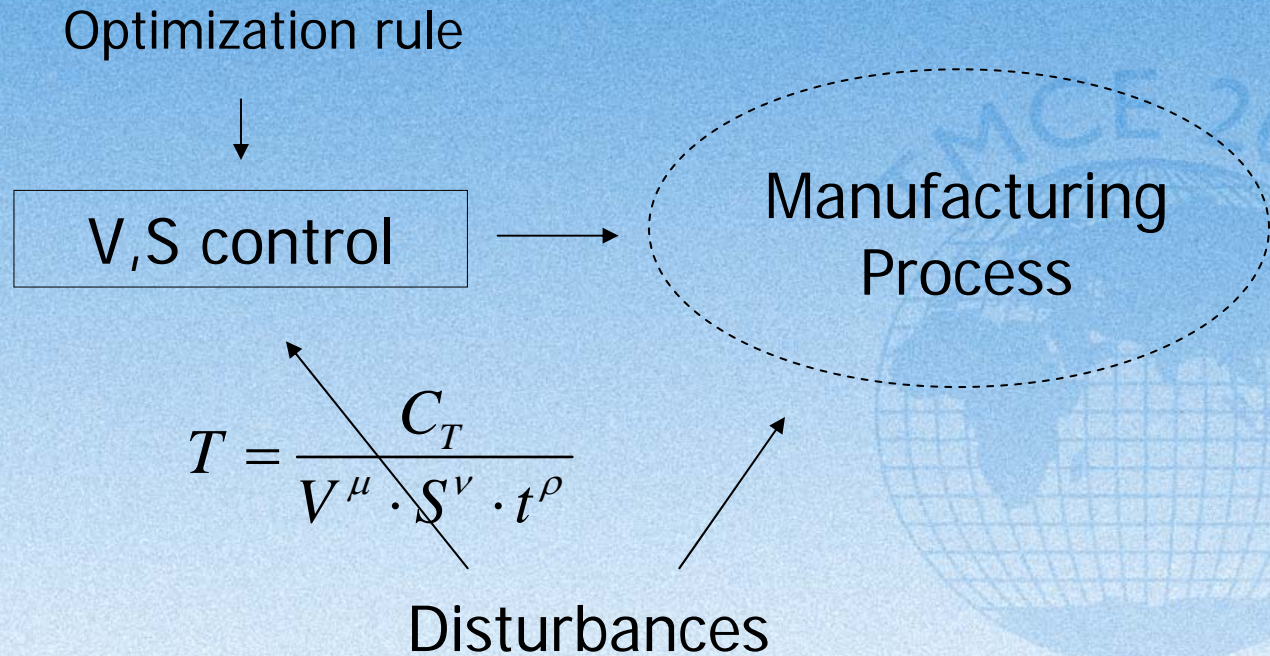
$V$  - Cutting speed

$S$  - Feedrate

$t$  - Depth of cut

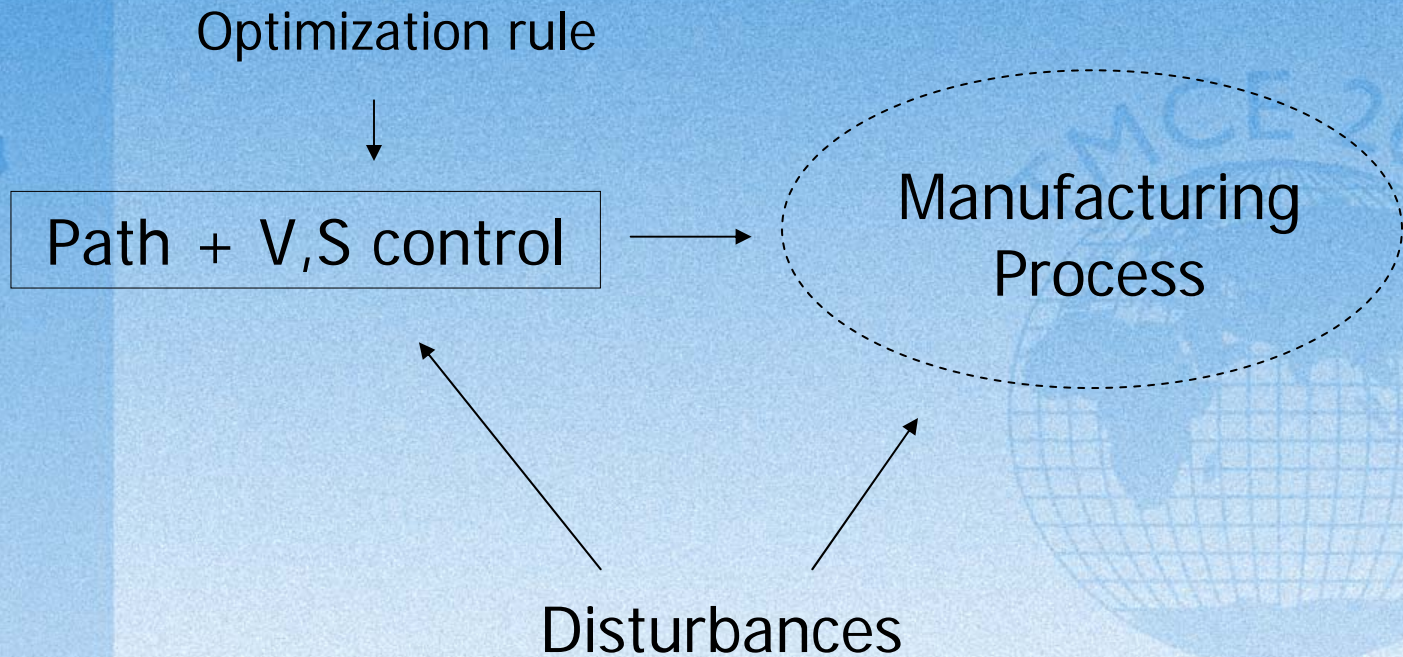
$$T = \frac{C_T}{V^\mu \cdot S^\nu \cdot t^\rho}$$

## Adaptive Real Time Control



$$T = \frac{C_T}{V^\mu \cdot S^\nu \cdot t^\rho}$$

## Adaptive Part Programming (APP)





$$T = \frac{C_T}{V^\mu \cdot S^\nu \cdot t^\rho}$$

## Research Concept

### Optimization Criteria

$$Q = \left( \tau_M + \frac{\tau_I}{N} \right) \cdot Q_T + \frac{Q_I}{N}$$

$$Q = \ell \cdot Z \cdot Q_T \cdot \left( \frac{1}{V \cdot S \cdot t} + \frac{\tau_I + Q_I / Q_T}{V \cdot S \cdot t \cdot T} \right)$$

$$q = \frac{1}{V \cdot S \cdot t} + \frac{\gamma}{C_T} \cdot V^{\mu-1} \cdot S^{\nu-1} \cdot t^{\rho-1}$$

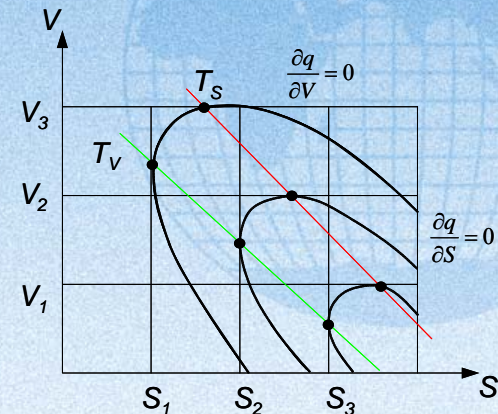
$$\gamma = \tau_I + \frac{Q_I}{Q_T}$$

$$\frac{\partial q}{\partial V} = 0 \quad \frac{\partial q}{\partial S} = 0 \quad \frac{\partial q}{\partial t} = 0$$



$$V^* = \left( \frac{C_T}{\gamma \cdot (\mu - 1) \cdot S^\nu \cdot t^\rho} \right)^{\frac{1}{\mu}}$$

$$S^* = \left( \frac{C_T}{\gamma \cdot (\nu - 1) \cdot V^\mu \cdot t^\rho} \right)^{\frac{1}{\nu}}$$



$$T = \frac{C_T}{V^\mu \cdot S^\nu \cdot t^\rho} \quad q = \frac{1}{V \cdot S \cdot t} + \frac{\gamma}{C_T} \cdot V^{\mu-1} \cdot S^{\nu-1} \cdot t^{\rho-1}$$

## Research Concept

### Optimization Criteria

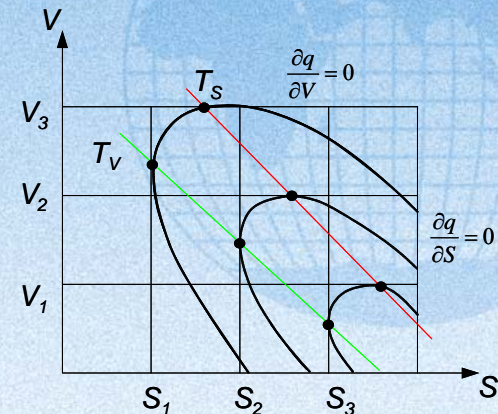
$$Q = \left( \tau_M + \frac{\tau_I}{N} \right) \cdot Q_T + \frac{Q_I}{N} \quad Q = \ell \cdot Z \cdot Q_T \cdot \left( \frac{1}{V \cdot S \cdot t} + \frac{\tau_I + Q_I / Q_T}{V \cdot S \cdot t \cdot T} \right)$$

$$q = \frac{1}{V \cdot S \cdot t} + \frac{\gamma}{C_T} \cdot V^{\mu-1} \cdot S^{\nu-1} \cdot t^{\rho-1} \quad \gamma = \tau_I + \frac{Q_I}{Q_T}$$

$$\frac{\partial q}{\partial V} = 0 \quad \frac{\partial q}{\partial S} = 0 \quad \frac{\partial q}{\partial t} = 0$$

$$V^* = \left( \frac{C_T}{\gamma \cdot (\mu - 1) \cdot S^\nu \cdot t^\rho} \right)^{\frac{1}{\mu}}$$

$$S^* = \left( \frac{C_T}{\gamma \cdot (\nu - 1) \cdot V^\mu \cdot t^\rho} \right)^{\frac{1}{\nu}}$$



$$T = \frac{C_T}{V^\mu \cdot S^\nu \cdot t^\rho} \quad q = \frac{1}{V \cdot S \cdot t} + \frac{\gamma}{C_T} \cdot V^{\mu-1} \cdot S^{\nu-1} \cdot t^{\rho-1}$$

## Research Concept

### Optimization Criteria

$$C_{m_i} \cdot V^\alpha \cdot S^\beta \cdot t^\gamma = M_i \leq [\Pi_i] \quad - \text{Boundary conditions}$$

$$\begin{array}{c} \downarrow \\ \left[ \begin{array}{l} H = C_H \cdot V^{\alpha_H} \cdot S^{\beta_H} \cdot t^{\gamma_H} \\ \Phi = C_\Phi \cdot V^{\alpha_\Phi} \cdot S^{\beta_\Phi} \cdot t^{\gamma_\Phi} \end{array} \right] \end{array} \longrightarrow q = a \cdot t^\eta + \frac{\gamma}{C_T} \cdot b \cdot t^\lambda$$

$$a = \frac{\{[H] \cdot C_H^{-1}\}^{(1/\beta_H)} \cdot (\beta_\Phi / \alpha_\Phi^{-1})}{\{[\Phi] \cdot C_\Phi^{-1}\}^{1/\alpha_\Phi}}$$

$$b = \frac{\{[\Phi] \cdot C_\Phi^{-1}\}^{(\mu-1)/\alpha_\Phi}}{\{[H] \cdot C_H^{-1}\}^{(1/\beta_H) \cdot (\beta_\Phi \cdot \mu / \alpha_\Phi - \beta_\Phi / \alpha_\Phi^{-1})}}$$

$$\eta = \frac{\gamma_\Phi}{\alpha_\Phi} + \frac{\gamma_H}{\beta_H} - 1 - \frac{\gamma_H \cdot \beta_\Phi}{\gamma_\Phi \cdot \beta_H}$$

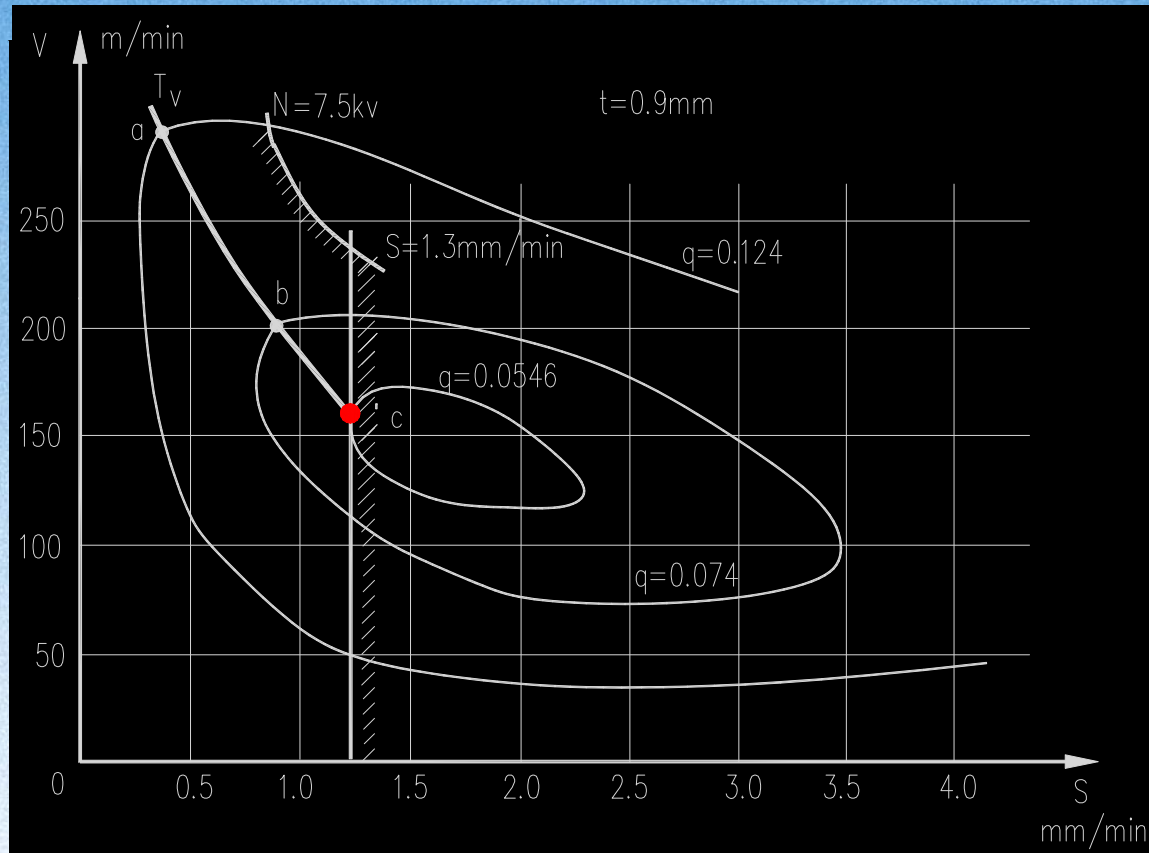
$$\lambda = \left( \frac{\gamma_H \cdot \beta_\Phi}{\alpha_\Phi \cdot \beta_H} - \frac{\gamma_\Phi}{\alpha_\Phi} \right) \cdot (\mu - 1) - \frac{\gamma_H}{\beta_H} \cdot (\nu - 1) + \rho - 1$$



$$T = \frac{C_T}{V^\mu \cdot S^\nu \cdot t^\rho} \quad q = \frac{1}{V \cdot S \cdot t} + \frac{\gamma}{C_T} \cdot V^{\mu-1} \cdot S^{\nu-1} \cdot t^{\rho-1}$$

## Research Concept

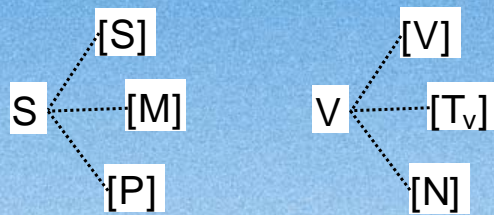
### Optimization Rules



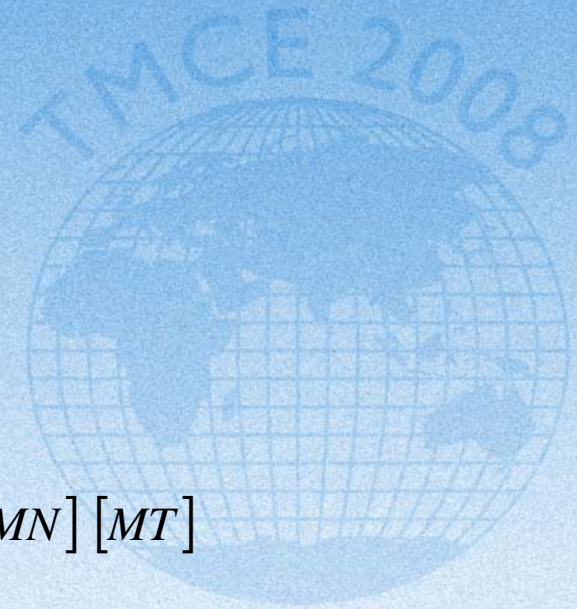
$$T = \frac{C_T}{V^\mu \cdot S^\nu \cdot t^\rho} \quad q = \frac{1}{V \cdot S \cdot t} + \frac{\gamma}{C_T} \cdot V^{\mu-1} \cdot S^{\nu-1} \cdot t^{\rho-1} \quad [PV][SV][PT][ST][SN][PN][MV][MN][MT]$$

## Research Concept

### Optimization Rules



$[PV][SV][PT][ST][SN][PN][MV][MN][MT]$



$$T = \frac{C_T}{V^\mu \cdot S^\nu \cdot t^\rho} \quad q = \frac{1}{V \cdot S \cdot t} + \frac{\gamma}{C_T} \cdot V^{\mu-1} \cdot S^{\nu-1} \cdot t^{\rho-1} \quad [PV][SV][PT][ST][SN][PN][MV][MN][MT]$$

## Research Concept

### 5 Typical cases of machining:

Workpiece - P20HB180; Cutting tool – GC415;  
 $\tau_I = 2\text{min}$ ;  $Q_I = 6.7\text{cent}$ ;  $[P_z] = 30\text{n}$ ;  $[P_y] = 4\text{n}$ ;  
 $[R_z] = 0.002\text{mm}$

Workpiece - K20HB260; Cutting tool – GC43  
 $\tau_I = 2\text{min}$ ;  $Q_I = 6.7\text{cent}$ ;  $[P_z] = 30\text{n}$ ;  $[P_y] = 7\text{n}$ ;  
 $[R_z] = 0.002\text{mm}$

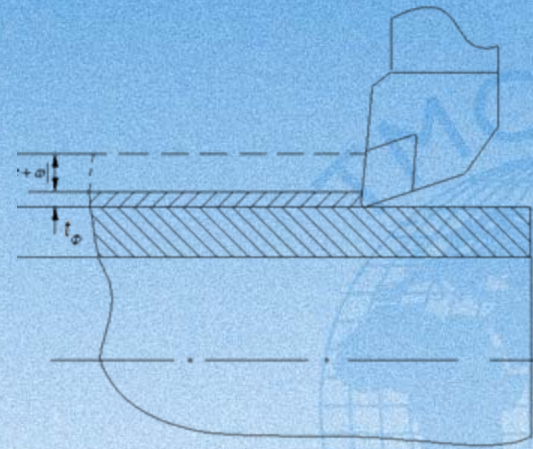
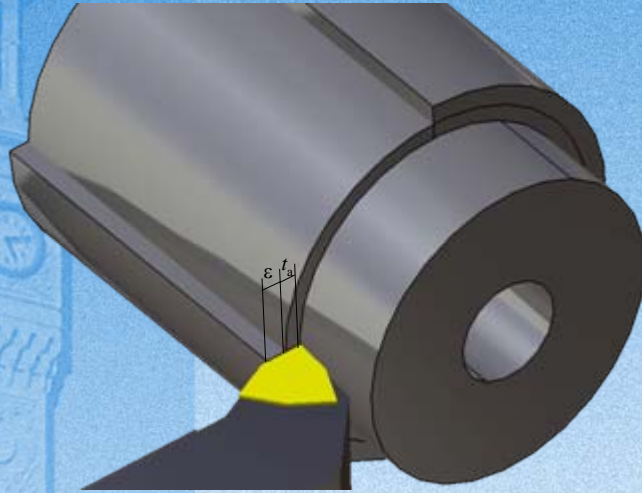
Workpiece – P30HB200; Cutting tool – GC415;  
 $\tau_I = 2\text{min}$ ;  $Q_I = 6.7\text{cent}$ ;  $[P_z] = 30\text{n}$ ;  $[P_y] = 7\text{n}$ ;  
 $[R_z] = 0.002\text{mm}$

Workpiece – P01HB100; Cutting tool – GC415;  
 $\tau_I = 2\text{min}$ ;  $Q_I = 6.7\text{cent}$ ;  $[P_z] = 30\text{n}$ ;  $[P_y] = 7\text{n}$ ;  
 $[R_z] = 0.002\text{mm}$

Workpiece - M20HB170; Cutting tool – GC435;  
 $\tau_I = 2\text{min}$ ;  $Q_I = 6.7\text{cent}$ ;  $[P_z] = 25\text{n}$ ;  $[P_y] = 7\text{n}$ ;  
 $[R_z] = 0.002\text{mm}$

$$T = \frac{C_T}{V^\mu \cdot S^\nu \cdot t^\rho} \quad q = \frac{1}{V \cdot S \cdot t} + \frac{\gamma}{C_T} \cdot V^{\mu-1} \cdot S^{\nu-1} \cdot t^{\rho-1} \quad [PV][SV][PT][ST][SN][PN][MV][MN][MT]$$

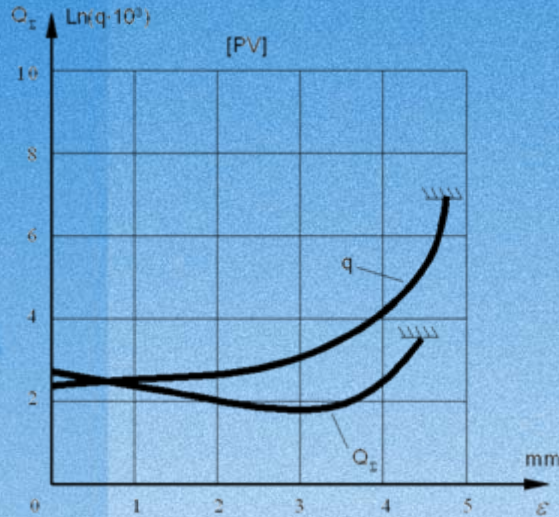
## Analysis of Adaptive Control





$$T = \frac{C_T}{V^\mu \cdot S^\nu \cdot t^\rho} \quad q = \frac{1}{V \cdot S \cdot t} + \frac{\gamma}{C_T} \cdot V^{\mu-1} \cdot S^{\nu-1} \cdot t^{\rho-1} \quad [PV][SV][PT][ST][SN][PN][MV][MN][MT]$$

## Analysis of Adaptive Control



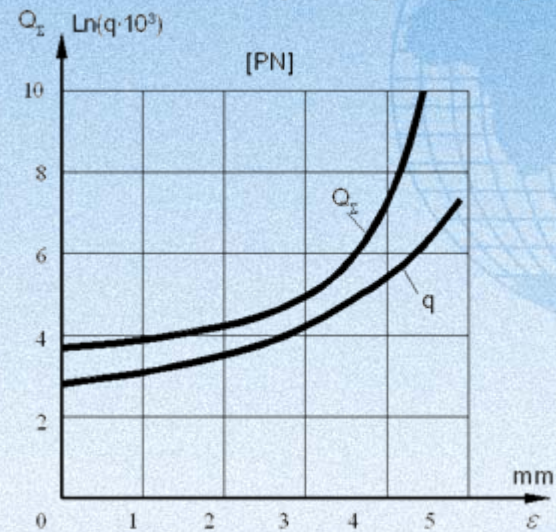
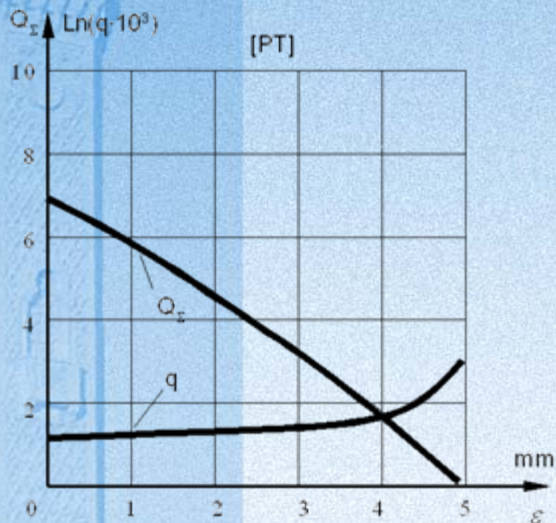
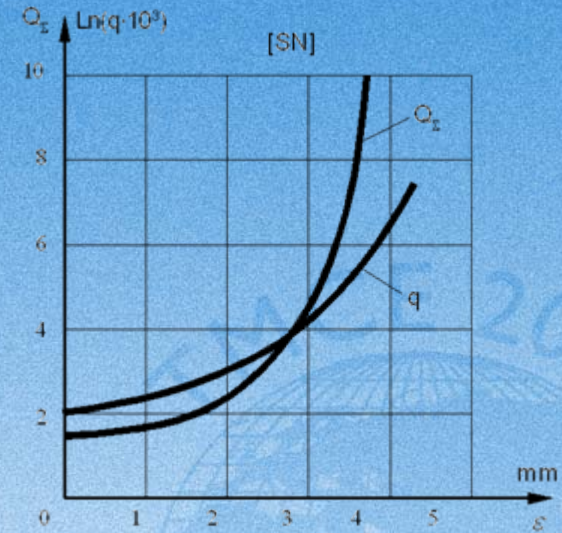
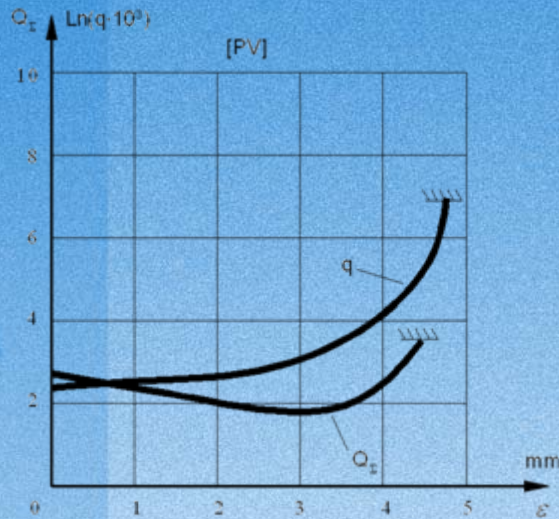
$$q \rightarrow Q_w$$

$$q = \frac{1}{V \cdot S \cdot t} + \frac{\gamma}{C_T} \cdot V^{\mu-1} \cdot S^{\nu-1} \cdot t^{\rho-1}$$



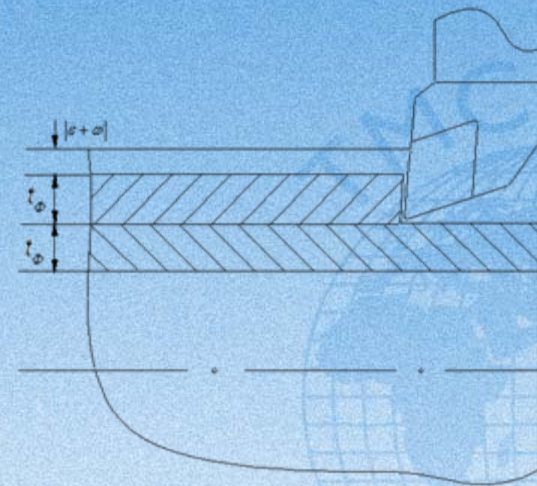
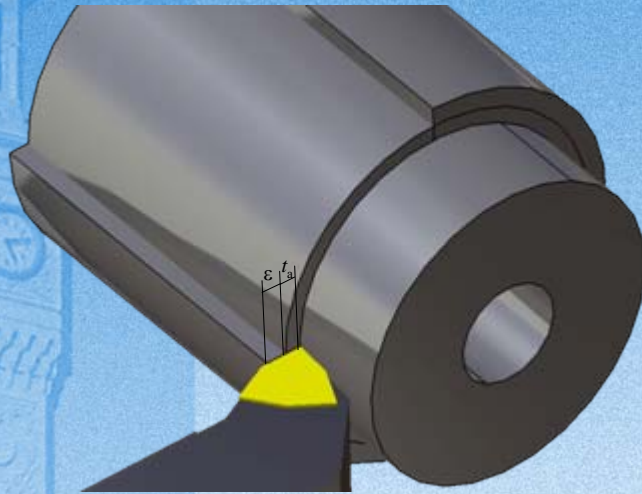
$$T = \frac{C_T}{V^\mu \cdot S^\nu \cdot t^\rho} \quad q = \frac{1}{V \cdot S \cdot t} + \frac{\gamma}{C_T} \cdot V^{\mu-1} \cdot S^{\nu-1} \cdot t^{\rho-1} \quad [PV][SV][PT][ST][SN][PN][MV][MN][MT]$$

## Analysis of Adaptive Control



$$T = \frac{C_T}{V^\mu \cdot S^\nu \cdot t^\rho} \quad q = \frac{1}{V \cdot S \cdot t} + \frac{\gamma}{C_T} \cdot V^{\mu-1} \cdot S^{\nu-1} \cdot t^{\rho-1} \quad [PV][SV][PT][ST][SN][PN][MV][MN][MT]$$

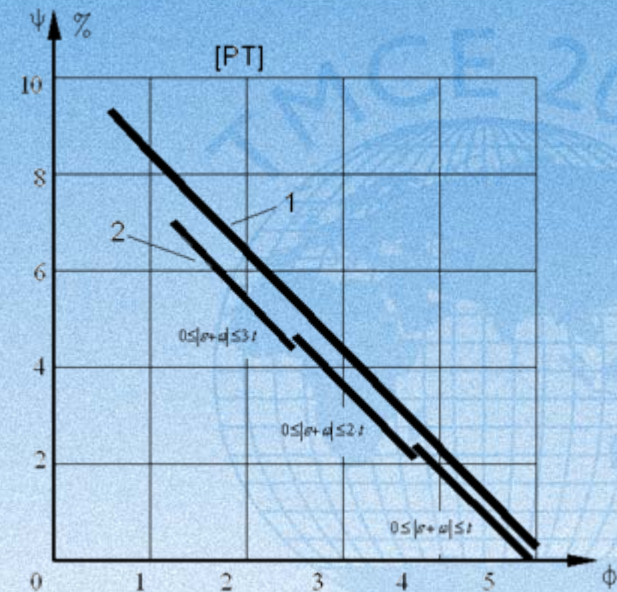
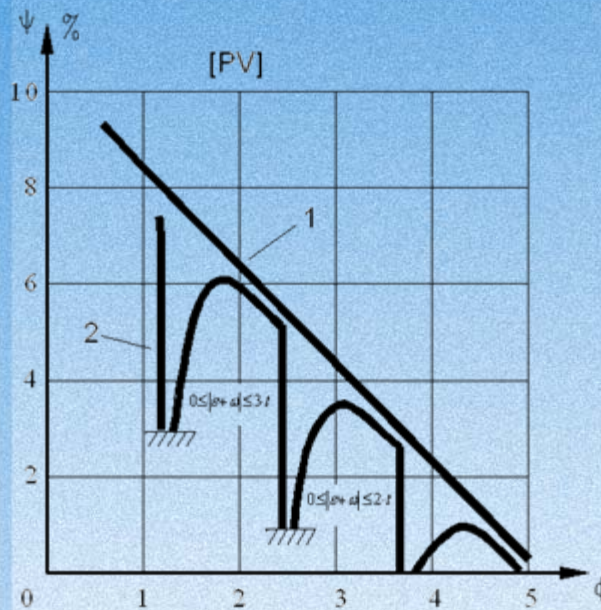
## Analysis of Adaptive Part Programming



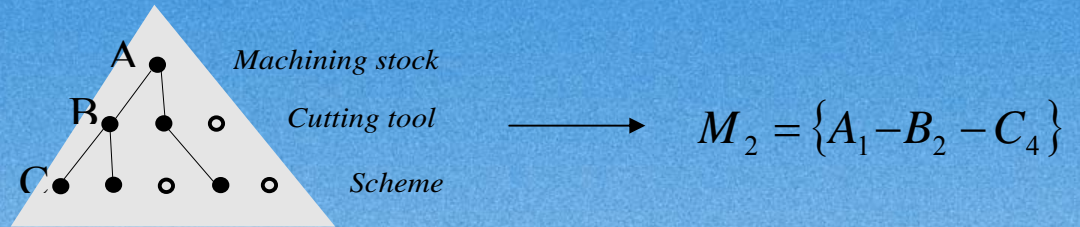
$$T = \frac{C_T}{V^\mu \cdot S^v \cdot t^\rho} \quad q = \frac{1}{V \cdot S \cdot t} + \frac{\gamma}{C_T} \cdot V^{\mu-1} \cdot S^{v-1} \cdot t^{\rho-1} \quad [PV][SV][PT][ST][SN][PN][MV][MN][MT]$$

## Analysis of Adaptive Part Programming

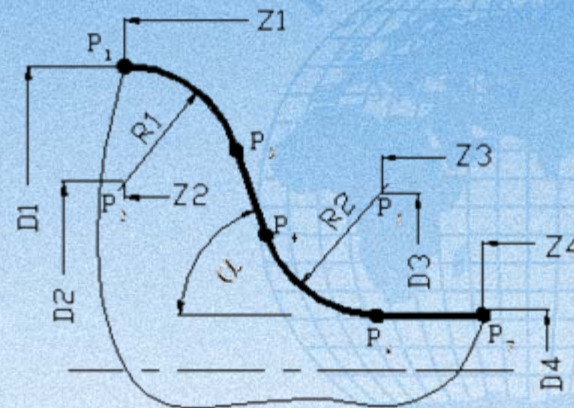
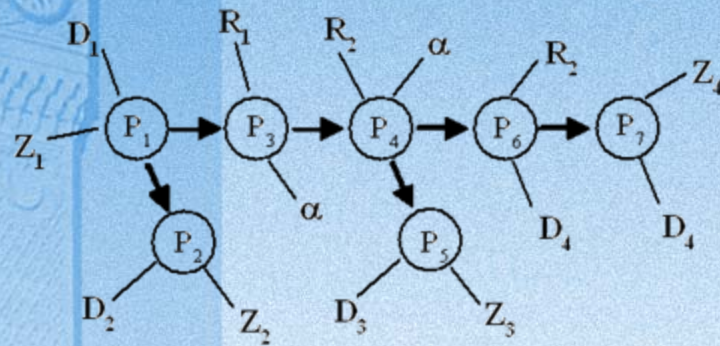
$$\psi = \left( \frac{Q_0}{Q_a} - 1 \right) \cdot 100\%$$



# Realization of APP

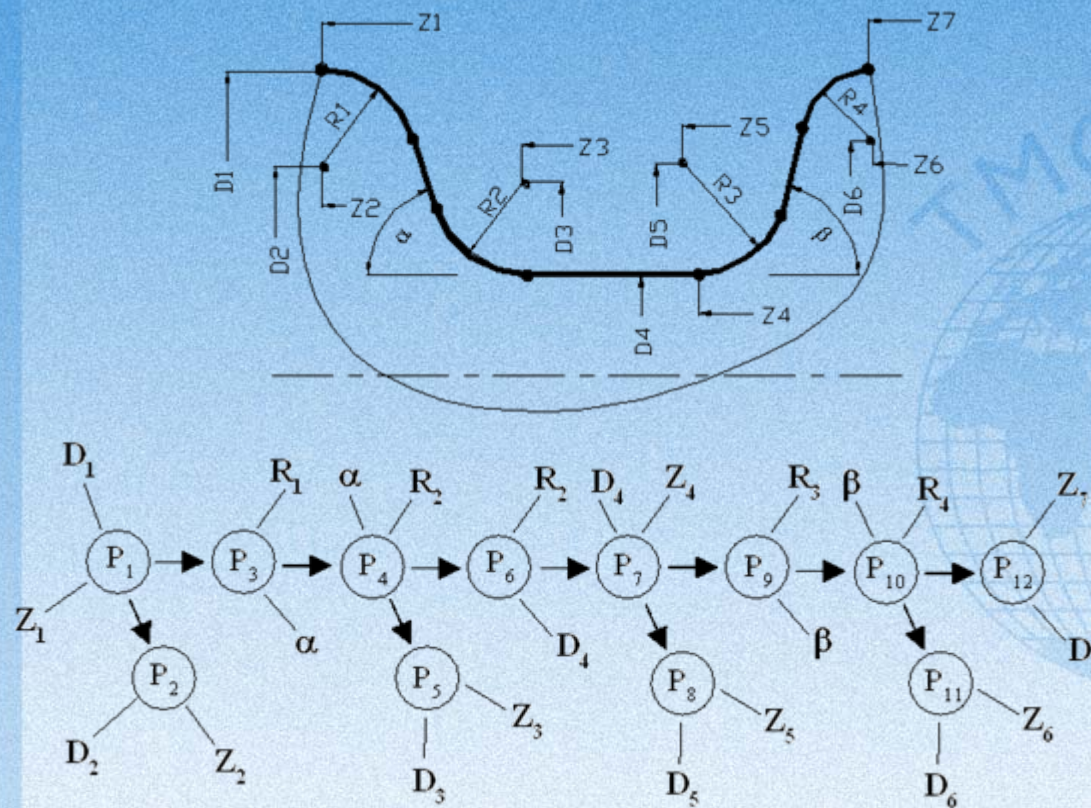


## STHO Structure



# Realization of APP

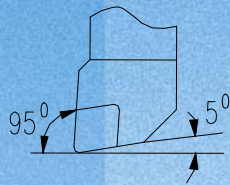
## STCL Structure



# Realization of APP

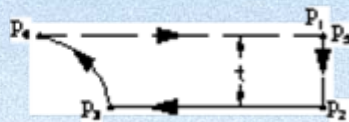
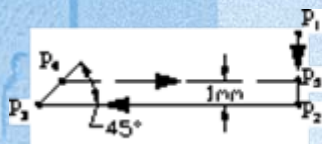
## Model Formalizm for STHO

$T_{1HO}$



$M_{1-1}$  – “Fast->Feedrate->Fast->Fast”

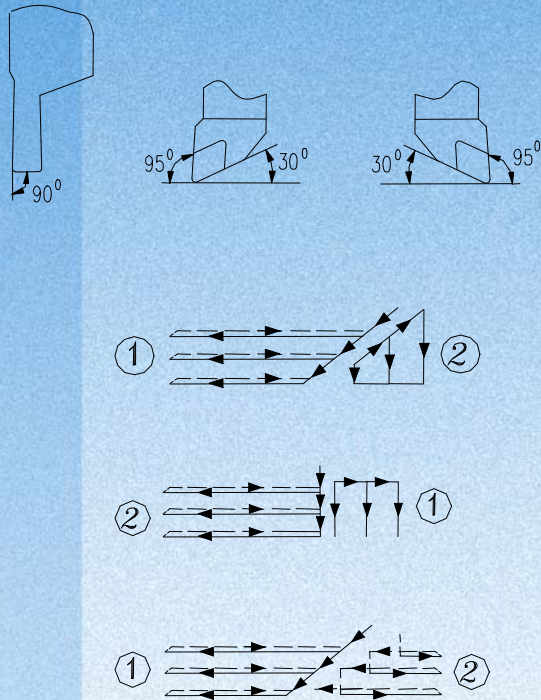
$M_{1-2}$  – “Fast->Feedrate->Feedrate->Fast”



$$\begin{matrix} Z_{HO}^E \rightarrow T_{1HO}^E \rightarrow M_{1-1}^L \\ Z_{HO}^E \rightarrow T_{1HO}^E \rightarrow M_{1-1}^D \\ Z_{HO}^E \rightarrow T_{1HO}^E \rightarrow M_{1-2}^L \\ Z_{HO}^E \rightarrow T_{1HO}^E \rightarrow M_{1-2}^D \end{matrix}$$

# Realization of APP

## Model Formalizm for STCL



$$\begin{array}{l}
 Z_{CL}^E \rightarrow T_{1CL}^E \rightarrow M_3 \\
 Z_{CL}^E \rightarrow T_{2HO}^E \rightarrow M_{1-1} \\
 \quad \quad \quad T_{1CL}^E \rightarrow M_3 \\
 Z_{CL}^E \rightarrow T_{1CL}^E \rightarrow M_3 \\
 \quad \quad \quad T_{1HO}^E \rightarrow M_{1-1} \\
 Z_{CL}^E \rightarrow T_{2HO}^E \rightarrow M_{1-1} \\
 \quad \quad \quad T_{2CL}^E \rightarrow M_{1-1}
 \end{array}$$



# CNC Custom Software Development

*Sinumerik MS2-300* Heidenhain Co.

Contact Probe *Marpos*

*Adaptive Control Unit Promess* – [M] [V]

$N \dots \{A_i\} \{X_j\} \{H_k\} \{Y_m\}$

$A_i$  - is array of subroutine names – 5 names  
L71÷L75 were reserved for this array

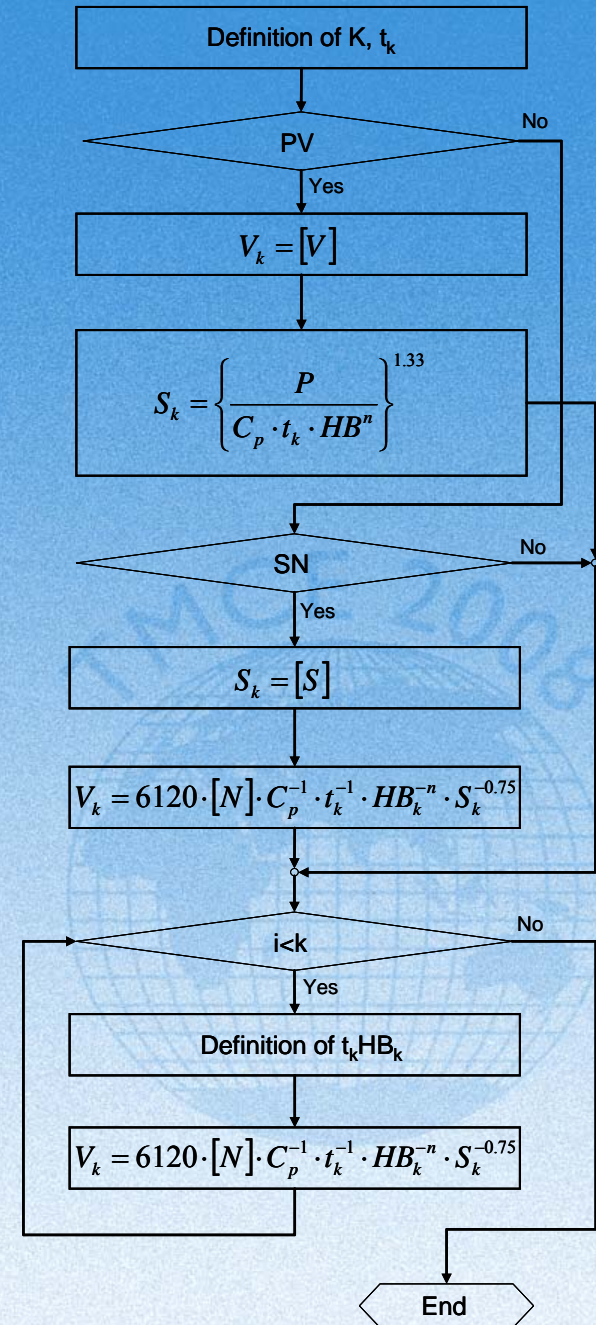
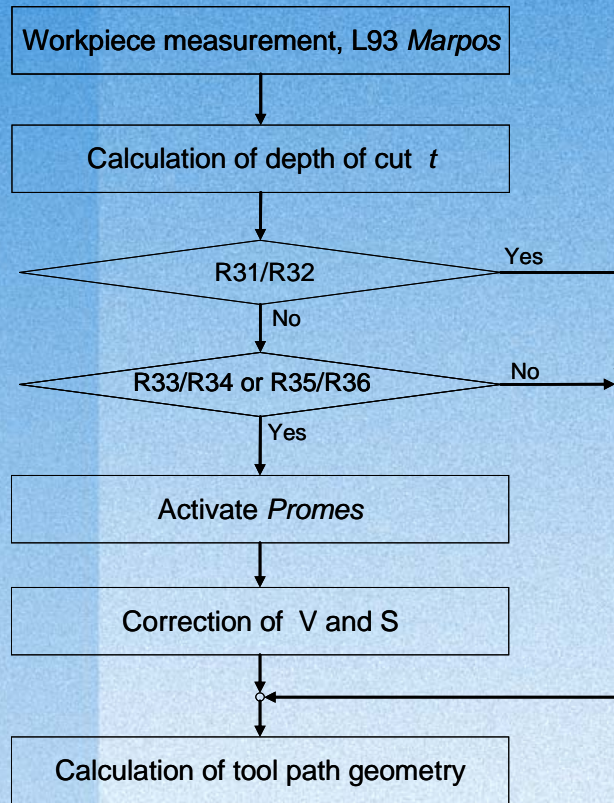
$X_j$  - array of geometrical parameters of  
STHO/STCL; 19 parameters R11÷R30 were  
reserved

$H_k$  - array of machining parameters,  
optimization rules and constants – 9  
parameters R31÷R40 were reserved

$Y_m$  - array of entry control parameters - 9  
parameters R41÷R50 were reserved.

# CNC Custom Software Development

## Correction Algorithms



# Conclusions

1. For rough cutting conditions it is identified that correction of tool path geometry according to actual value of workpiece dimensions brings enhancement of fixed rule adaptive control for  $[PV]$ ,  $[SN]$ ,  $[PN]$ ,  $[MV]$ ,  $[MN]$  control.
2. For limitations concerning with cutting tool life period (rules  $[PT]$ ,  $[MT]$ ), correction of tool path geometry is not necessary.
3. Adaptive Part Programming approach can be realized through the customization of the standard cycle's library of CNC.

Thanks a lot !

